Modeling effects of harvest on firefly population persistence

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A B S T R A C T

North American fireflies in the genus Photinus are commercially harvested to extract the enzyme luciferase, despite the availability of a synthetic recombinant enzyme. Our goal was to examine the potential effects of harvesting on Photinus population persistence. Using estimated demographic parameters for Photinus, we developed a stochastic simulation population model to understand combined effects of demography, harvest rate, delayed larval development, and environmental stochasticity on population persistence of fireflies. With no harvest and low environmental stochasticity, modeled populations tended to reach carrying capacity. We found that average population size of adult fireflies decreased with increasing harvest rate and increasing environmental stochasticity. At the highest modeled growth rate (λ = 2.8) the population failed to persist only when environmental stochasticity was high and harvest rate was ≥ 60%. Once harvest was introduced, only populations with high growth rates consistently persisted. Long-term, sustainable Photinus harvest rates based on survey data suggest that harvest rates >10% are acceptable only if λ > 1.6. Our modeling results suggest that Photinus populations might tolerate low harvest levels, although in the absence of more precise data on vital rates and the amount of environmental stochasticity, the exact level is unknown. To further examine sustainability, harvest rates should be monitored and standardized surveys conducted to document firefly population changes.

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1. Introduction

One of the most common causes of current species extinctions is overharvest, or overkill (Brook et al., 2008; Yiming and Wilcove, 2005). The effect of harvest on population viability is central to hunting and other sustained yield programs and has been well studied for species of commercial concern, mostly vertebrates and trees (e.g., Ellen and Fieberg, 2003; Gustafson, 1996; Taylor et al., 2005). Many efforts have been made to determine sustainable harvesting practices for species commonly collected or exploited by human commerce, such as wild fish (Conover and Munch, 2002), parrots (Beissinger and Bucher, 1992), and sharks (Gallucci et al., 2006). Sustainable harvest practices for invertebrates have received less attention (Dunn, 2005). Most invertebrate harvesting studies have focused on commercial species that humans use as food or bait, such as abalone, oysters, crabs, tunicates, sponges, and annelids (New, 1995; Reynolds et al., 2001). There are many insect groups harvested for taxonomic collections, such as birdwing butterflies, Papilionidae (Marshall, 1982; Owen, 1971) and beetles, Coleoptera (New, 1995). However, effects of such harvest on population persistence have seldom been quantified, and current insect harvest practices are considered by some to be unsustainable (e.g., butterflies, Kurdina, 1986; Petanidou et al., 1991; USFWS, 1997).

Fireflies (Coleoptera: Lampyridae) are charismatic insects that attract considerable public attention. Firefly harvesting has been virtually ignored, despite recent concerns about their conservation status (Takeda et al., 2006). The bioluminescent displays of certain synchronously flashing fireflies appeal to ecotourists (e.g., Photinus carolinus in Great Smoky Mountains National Park, USA (Faust, 2010), Pteroptyx tener in Kuala Selangor, Malaysia (Wong and Yeap, 2012)). There have been widespread reports of declining firefly populations (Khoo et al., 2009; Wong and Yeap, 2012; L.F. Faust, unpubl. data), although the lack of systematic monitoring means that most evidence is anecdotal. Although purported firefly declines might be partially attributed to habitat destruction, pesticides, and light pollution, overharvest may also have a substantial impact. In the USA, fireflies are harvested commercially to extract luciferase (Howes, 1993; Sigma-Aldrich, 2010), an enzyme that catalyzes light production when adenosine triphosphate (ATP) is present. Until 1985, luciferase could be obtained...
only by harvesting live fireflies (mainly Photinus spp. in the USA), but once the Photinus pyralis luciferase gene was cloned (de Wet et al., 1985) synthetic luciferase could be produced in large quantities.

Although it is no longer necessary to harvest fireflies to extract luciferase, commercial firefly harvesting continues. For example, during the summer of 2008 collectors in one Tennessee county reportedly harvested 1584 g of fireflies (The Oak Ridger, 2008). At approximately 40 mg wet weight per Photinus individual (S. Lewis, unpubl. data), this represents approximately 40,000 male fireflies. Harvesting has the potential to impact Photinus firefly populations in the USA, but no studies have evaluated what harvest levels these insect populations can sustain. Here we use a pattern-oriented modeling approach (e.g., Grimm et al., 1996; Wichmann et al., 2003) to examine the potential effects of harvest on firefly population size and persistence. Because stochasticity affects population persistence, we first developed a deterministic model to allow us to investigate the effects of variation in demography and harvest rate on population growth and equilibrium population size. We then included demographic stochasticity but kept the environment constant, followed by adding environmental stochasticity to determine the combined influence of both sources of stochasticity on population persistence. We next examined how different larval development strategies might affect population persistence. Finally, we performed a sensitivity analysis to evaluate which of our estimated parameters has the greatest impact of population persistence.

2. Methods

2.1. The model

We developed a stage-structured model of an insect population that has a single reproductive period per year, after which adults die. The model includes harvest of adults of both sexes, although in some species of Photinus only the males are harvested. Eggs usually develop into adults within a single year, but the model allows for prolonged larval development, as seen in some species, where some larvae take more than one year to reach adulthood (e.g., Hovestadt et al., 2007). Because we used the model to analyze the consequences of extending the larval stage beyond a single year, only a fraction of larvae become adults after one year. We used the model to investigate how population persistence is affected if larvae postpone development with a fixed probability, e.g. as a diversified bet-hedging strategy (Philippi and Seger, 1989), and if the delayed larval development is a result of phenotypic plasticity caused by environmental signals (Danforth, 1999; Danks, 1992). Finally, the model incorporates the probability that adult females become mated, to allow us to investigate one type of Allee effect when population density becomes low.

As the purpose of the model is to investigate the risk of population extinction due to harvesting, we included demographic stochasticity by considering population size as a discrete stochastic variable affected by probabilistic demographic events. We added increasing levels of environmental stochasticity to the model, thereby enabling us to explore whether prolonged larval development is a beneficial strategy in an unpredictable environment.

In our model, we considered three developmental stages in the life cycle of fireflies: eggs (E), larvae (L) and adults (A). Adults consist of females (A_f) and males (A_m), and larvae consist of those that have spent approximately i years in the larval stage (L_i), so that L = \sum_{i=1}^{\Psi} L_i, where \Psi is the maximum number of years an individual can spend in the larval stage.

2.2. Deterministic model

The number of eggs produced by A_f adult females in year t is denoted E(t), and the expected number of young larvae that will develop from these eggs is

$$L_0(t) = p_E E(t)$$

where p_E is the probability that an egg develops into a larva.

The probability that a larva survives the first year is denoted p_{1l}.

We determined that a proportion of surviving larvae do not pupate and therefore start on their second larval year (denoted b). Larvae that do not emerge after the second year die. Thus, the number of larvae that are approximately one-year old in the following year becomes

$$L_1(t + 1) = p_{1l}bL_0(t)$$

while the number of two-year old larvae in year t + 1 is the number of one-year old larvae that remain larvae and survive for an extra year, i.e.

$$L_2(t + 1) = p_{1l}b_1L_1(t)$$

or, in general, for individuals spending i + 1 year in the larval stage as

$$L_{i+1}(t + 1) = p_{1l}b_iL_i(t)$$

We assumed that the probability of a larva surviving from one year to the next declines with larval density due to intraspecific interactions such as competition for resources and cannibalism (Evans, 1991; Inouye, 1999; Lee and Seybold, 2010; Miller, 1964; Peckarsky, 1991). A general model for the decrease in survival rate of larvae during their ith year is

$$p_{il} = p_{mi} \exp \left( -\sum_{j=0}^{\Psi} c_{ij}L_j \right)$$

where p_{mi} is the survival rate of age i larvae in the absence of intraspecific competition. c_{ij} expresses the influence of competition on survival rate exerted by larvae of age j on larvae of age i.

Larval competition may prolong development time (Danks, 1992; Gerber, 1984), so the proportion of larvae taking an extra year to develop will increase with population size. We modeled the proportion of larvae postponing pupation as

$$b_i = 1 - (1 - b_{mi}) \exp \left( -\sum_{j=0}^{\Psi} c_{ij}L_j \right)$$

where b_{mi} is the proportion of larvae of age i that do not pupate in the absence of intraspecific competition and \delta_i is a constant expressing the effect of competition on development of larvae. Note that by varying b_{mi} and \delta_i, Eq. (6) can model delayed larval development as a fixed proportion of all larva (when b_{mi} > 0 and \delta_i = 0), as a variable proportion dependent on larval density (when b_{mi} = 0 and \delta_i > 0), as a mixture of the two strategies (when b_{mi} > 0 and \delta_i > 0), or as the absence of developmental delay (when b_{mi} = 0 and \delta_i = 0).

In year t + 1, expected recruitment of adults comes from larvae that have spent one or more years in that stage. The probability that a larva survives pupation and reaches reproductive maturity is denoted p_{A_r}, so the expected number of adults in year t + 1 is

$$A(t + 1) = \sum_{i=1}^{\Psi} (1 - b_i)p_{A_r}L_i(t + 1)$$

of which A_f(t + 1) = fA(t + 1) are females and A_m(t + 1) = (1 - f)A(t + 1) are males (0 \leq f \leq 1).
The maximum number of eggs a female can produce under optimal conditions is denoted $F_m$. It declines if the number of males is inadequate to ensure that all females lay their full complement of eggs. We used Holling's (1959) disc equation to model the expected number of matings per male ($m$) during a breeding season of length $T$, i.e.

$$m = \frac{a(1 - (1 - \tau)h_f)A_f T}{1 + atm(1 - (1 - \tau)h_f)A_f}$$

(8)

where $A_f$ is the number of adult females emerging in a given year, $a$ is a constant expressing how efficient the males are in finding females, and $tm$ is the time needed per copulation. $a$, the efficiency of males finding females, can be affected by a variety of factors including population density, operational sex ratio, temperature, wind, and precipitation (Faust, 2012). $h_f$ is the proportion of females harvested, and $\tau$ is the timing of harvest. Thus, $\tau$ would be 0.0, 0.5, or 1 if harvesting takes place before, during, or after the mating season, respectively. For our purposes, we only modeled $\tau = 0$. We define the effective harvest rate, i.e. the impact harvest has on the number of reproductive females, as $h_f' = (1 - \tau)h_f$. Likewise, we define the effective harvest rate of males as $h_m' = (1 - \tau)h_m$ where $h_m$ is the proportion of adult males being harvested. As the total number of matings is $m(1 - h_m')A_m$, the mean number of matings per female therefore becomes

$$\mu = \frac{m(1 - h_m')A_m}{(1 - h_f')A_f} = \frac{a(1 - h_m')A_m}{1 + atm(1 - h_f')A_f}$$

(9)

We assume that a mated female can produce up to $F_m$ eggs, while unmated females produce none. The proportion of unmated females is calculated from the 0-term of the Poisson distribution as $e^{-\mu}$. The mean fecundity per female is assumed to increase with the proportion of females that have mated at least once during their lifetime, i.e. $1 - e^{-\mu}$. Thus, the expected fecundity per female is

$$E(t + 1) = F_m(1 - e^{-\mu})$$

yielding the expected total number of eggs in year $t + 1$ as

$$E(t + 1) = F(t + 1)(1 - h_f')A_f(t + 1)$$

(11)

2.3. The stochastic version of the model

Demographic stochasticity was incorporated by replacing expected values with integer values obtained from probability distributions. Hence, the number of newly hatched larvae in year $t$ is found as

$$L_0(t + 1) = \text{Bin}(p_e, E(t))$$

(12)

which means that the number of larvae is generated from a binomial distribution with parameters $p_e$ and $E(t)$ by means of Monte Carlo simulation. The number of larvae surviving to the next year is generated as

$$L_{i+1}(t + 1) = \text{Bin}(p_i, L_i(t)) \quad \text{for} \quad i = 0, 1, 3, \ldots, \psi$$

(13)

Of surviving larvae, the number of pupating larvae is generated as $\text{Bin}(1 - b_{i+1}, L_{i+1}(t + 1))$ and the number of adults ($A(t + 1)$) is generated from a binomial distribution with survival probability $p_o$.

The numbers of reproducing adult males and females are modeled as

$$A_m(t + 1) = \text{Bin}(1 - h_m', A_m(t + 1))$$

(14a)

and

$$A_f(t + 1) = \text{Bin}(1 - h_f', A_f(t + 1))$$

(14b)

The total number of eggs produced is assumed to be Poisson distributed i.e.

$$E(t + 1) = \text{Poisson}(F(t + 1)A_f(t + 1))$$

(15)

where $F(t + 1) = F_m(1 - \exp \left(-\frac{atA_m}{1 + atm(1 - h_f')A_f}\right))$

Environmental stochasticity can affect the values of the model’s parameters, so instead of regarding them as fixed values, they can be replaced by probability distributions. However, we incorporated stochasticity into only the parameters we considered important for the dynamics of a species. For instance, in the case of Photinus pyralis we assumed that the most critical phase in the species' life cycle is during summer, when males search for females to mate with. In ‘poor’ breeding seasons, which are characterized by cold, rainy weather during early summer or hot, dry weather during late summer, activity of males declines causing fewer females to be mated (Faust, 2010, 2012; S. Lewis pers. obs.). As mating rate depends on the parameter $a$ in Eq. (8), we can let a vary stochastically from year to year. In poor summers, $a$ may be close to 0 and in ‘good’ summers (‘good’ referring to high mating success) it may be close to its maximum value denoted $a_m$. Assuming that $a$ varies randomly and symmetrically around a mean (or median) value (denoted $\bar{a}$), we can replace $a_m$ with $2\bar{a}$ and model the actual value of $a$ in year $t$ as

$$a(t) = a_m + \bar{a}e^\varepsilon \quad 0 < a(t) < a_m$$

(16)

where $\varepsilon$ is a normally distributed stochastic variable with zero mean and standard deviation $\sigma$. Each year is characterized by a new random value of $\varepsilon$.

Likewise, if the parameter subject to environmental stochasticity is a probability rather than a rate, and therefore constrained to fall between 0 and 1, the time-specific probability in year $t$ can be modeled as

$$p(t) = \frac{\bar{p}e^\varepsilon}{1 + \bar{p}(e^\varepsilon - 1)} \quad 0 < p(t) < 1$$

(17)

where $\bar{p}$ denotes the median value of $p(t)$. The median and the mean values of $p(t)$ will be the same if $\bar{p} = 0.5$. This environmental stochasticity can be caused by increased rainfall, low temperatures, or drought, which can interrupt or shorten the mating season (Faust and Weston, 2009; Kaufmann, 1965).

2.4. Applying the model to firefly populations

Although many Photinus species are harvested for commercial purposes, vital rates were obtained from the relatively well-studied species Photinus ignitus (Craitsley and Lewis, 2005; Rooney and Lewis, 2002). Along with most Photinus species, $P$. ignitus is found throughout eastern North America during summer months (Faust and Weston, 2009; Lloyd, 1966). Females lay their eggs in the soil and larvae hatch after about two weeks. Singly mated females lay an average of $18.5 \pm 3.2$ (SD) eggs; increasing the number of mates increases the number of eggs laid (Rooney and Lewis, 2002). Egg survival has only been estimated in the lab, and that was 88–93% (Rooney and Lewis, 2002). This hatching rate is similar to the 93% egg survival rate reported in captive Photuris fulvipes (Rosa, 2007). Larvae then spend one to two years underground, subsisting on earthworms and soft-bodied insect larvae, but nothing is known about survival rates during this stage. Danks (1992) found that prolonged development can be caused by scarcity of food, but environmental factors such as temperature, photoperiod, and humidity may also be involved (Buschman, 1988; McLean et al., 1972; Rosa, 2007).

Pupation typically takes two weeks (Lewis and Lloyd, 2003), after which adults emerge and immediately begin breeding. The
Photinus ignitus adult lifespan is about two weeks (Cratsley et al., 2003; Lewis and Wang, 1991).

Adult Photinus population sizes are extremely variable from year-to-year, but generally do not appear to exceed several thousand individuals across an area ranging from 10 to 100 hectares (S. Lewis, unpubl. data), so in our simulations we set carrying capacity at 6000 adults, i.e. \( A(t + 1) = A(t) + \Lambda - \mu K \). Likewise, at equilibrium we have \( E(t + 1) = E(t) = E^* \), and \( L(t + 1) = L(t) = L^* \). This means that the number of eggs produced per year at equilibrium can be found as

\[
E^* = F_m(1 - e^{-\gamma_A}) \mu L = F_m \left(1 - \exp \left(-\frac{\mu(1 - f) KT}{1 + \alpha_{nm} K} \right)\right) fK
\]

(18)

From the published literature, we estimate that females, on average, are responsible for an average of 28 eggs \( F \) over the course of their lifetime. This value was calculated by taking into account the average number of matings a female receives (Cratsley et al., 2003), the probability of mating with males that have already mated (mating history influences spermatophore size), and the average fecundity of females receiving large or small spermatophores (Rooney and Lewis, 2002). The average male has two successful matings over the course of his lifetime (Cratsley et al., 2003), so we set \( m = 2 \). Furthermore, if we assume that the sex ratio is even \( (f = 0.5) \), and since \( m = \mu(1 - f)/f \), we find \( \mu = 2 \). Setting \( T \) equal to one mating season, \( t_m \) should be 0.333 if a male maximally mates three times during its lifespan (Rooney and Lewis, 2002). Finally, setting \( a(1 - f)K/(1 + \alpha_{nm} K) = 2 \) yields \( a = 0.002 \) per mating season. Finally, \( E^* = F_m(1 - e^{-\gamma_A}) \mu L = 28(1 - e^{-2})0.5 \times 6000 = 72,632 \) eggs.

We set the survival probability from egg to larval stage \( (p_L) \) at 89%, based on data from captive, laboratory individuals (Rooney and Lewis, 2002), so the number of young larvae at equilibrium becomes \( L^*_n = p_L E^* = 64,642 \).

The default parameter values associated with the larval stage were obtained by making following assumptions: (i) When a population is at equilibrium, 20% of the larvae spend an extra year in the soil (i.e. \( b_1 = b = 0.2 \)); (ii) Larvae can maximally spend two years in the soil \( (\Psi = 2) \); (iii) The competition factor \( (c_L) \) is the same for all larvae irrespective of age (i.e. \( c_L = c \)). From Eq. (5) we find the equilibrium value of \( p_L \) as

\[
p_L = \frac{p_m \exp \left( -\sum_{j=0}^{\Psi} c_L j \right)}{\sum_{j=0}^{\Psi} c_L j}
\]

(19)

\[
= p_m \exp(\psi c_L a_0 - cp_L b L_0(1 - t)) = p_m \exp(-c(1 + p_L b L_0^*)^*)
\]

We assume that the survival probability of a larva staying one year in the soil without competition with other larvae is 20%, i.e. the default value of \( p_L \) is 0.2.

The number of larvae becoming adults is

\[
A^* = p_L^* p_a (1 - b) L_0^* + (p_L^*)^2 b_p a L_0^* = K
\]

(20)

which means that \( p_L^* \) can be obtained as the largest positive root of

\[
p_L^* = \left(1 - b\right) \pm \sqrt{(1 - b)^2 + 4 b K/(p_a L_0^*)} / 2b
\]

(21)

when \( 0 < b < 1 \), while for \( b = 0 \) or \( b = 1 \), Eq. (20) reduces to \( p_L^* = K F_m / p_a L_0^* \) and \( p_L^* = \sqrt{K / p_a L_0^*} \), respectively. As we have no knowledge of \( p_a \) we will use \( p_a = 1 \) as the default value, but Eq. (21) shows that lower values of \( p_a \) will increase \( p_L^* \).

Finally, once \( p_L^* \) has been obtained from Eq. (21), the default value of \( c \) is found from Eq. (19) is

\[
c = \frac{1}{(1 + p_L^* b L_0^*) \ln \left( \frac{p_m}{p^*_L} \right)}
\]

(22)

As the default parameter values yield \( p_L^* = 0.1128 \), we get the default value of \( c \) as 0.000087.

The proportion of larvae spending two years in the soil \( (b) \) is modeled according to Eq. (6) as

\[
b = 1 - (1 - b_m) \exp(-\delta(1 + p_L^* b L_0^*))
\]

where \( \delta \) expresses the effect of larval competition on the developmental rate of larvae. If the developmental strategy is fixed, we set \( \delta = 0 \), so that \( b = b_m = 0.2 \). On the other hand, if it is either purely flexible or mixed, \( \delta \) can be obtained as

\[
\delta = \frac{1}{c(1 + p_L^* b L_0^*) \ln \left( \frac{1 - b_m}{1 - b} \right)} \quad (b_m < 1)
\]

(23)

If we assume that delayed larval development is purely flexible so that it occurs only when larvae compete for resources, we can set \( b_m = 0 \). Consequently, if 20% of the larvae spend an extra year in the soil when the population is at equilibrium, the default value of \( \delta \) is 0.3899.

2.5. Model scenarios

To solve the model numerically it was converted into a computer simulation model and implemented in Delphi 2009 (Embarcadero®). An executable version of the model, called Fireflies, is available by emailing gnachman@bio.ku.dk.

To estimate allowable harvest rate under a variety of conditions, we varied \( \lambda \), environmental stochasticity, and harvest rate. \( \lambda \) is defined as the finite growth rate of the population when there are no limiting factors for growth; that is, all females reproduce maximally \( (F = F_{\text{max}}) \), food is unlimited \( (p_m = p_m) \), there is no harvest \( (h = 0) \) and no environmental stochasticity \( (\sigma = 0) \). In this situation, from the deterministic version of the model,

\[
A(t + 1) = p_L^* p_a (1 - b) p_p a F_m A(t) + p_L^* p_m^2 b_p p_a F_m A(t - 1)
\]

(24)

The probabilities \( p_r \), \( p_m \), and \( p_a \) can be combined into a joint probability denoted as \( P = p_r p_m p_a (0 \leq P \leq 1) \). Thus, \( P \) expresses the probability that an individual survives from the egg stage to the adult stage if development takes a single year. Eq. (24) can therefore be written as

\[
A(t + 1) = P(1 - b) F_m A(t) + p_m B b F_m A(t - 1)
\]

As \( \lambda = A(t + 1)/A(t) \), we can find \( \lambda \) as the largest positive root of

\[
\lambda = \sqrt[2]{P(1 - b) F_m + 4P \sqrt{P(1 - b) F_m + 4P b F_m}}
\]

(25)

If \( b = 0 \) (i.e., life history is strictly univoltine), we get \( \lambda = P F_m \).

We varied vital rates to yield \( \lambda \)'s approximately equal to 1.2, 1.6, 2.0, 2.4, and 2.8. To limit the number of combinations, we only changed \( p_m \) and \( F_m \) (Supplementary Materials) while the remaining parameters took their default values (Table 1). Irrespective of \( \lambda \), the carrying capacity of the population was fixed to \( K = 6000 \) adults. The values of \( c \) and \( \delta \) necessary to keep the number of adults at a carrying capacity for a given combination of \( p_m \) and \( F_m \) were found by solving Eqs. (22) and (23).

We also investigated the effect of larvae with a strictly univoltine lifecycle, i.e. \( b = 0 \), with an unconditional strategy \( (b_m = 0 \) and \( \delta = 0) \), and with a purely conditional (density-dependent) strategy (i.e. \( b_m = 0 \) and \( \delta > 0 \)).

The effect of harvest was modeled by varying the proportion of adult males being removed from the population \( (h_m) \), whereas
Table 1: Default parameter values used in the simulation model. Values are estimated at population equilibrium.

<table>
<thead>
<tr>
<th>Parameter symbol</th>
<th>Description</th>
<th>Value(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K$</td>
<td>Carrying capacity of adults</td>
<td>6000</td>
</tr>
<tr>
<td>$p_h$</td>
<td>Hatching probability of eggs</td>
<td>0.89</td>
</tr>
<tr>
<td>$p_n$</td>
<td>Maximum survival probability of larvae</td>
<td>0.2</td>
</tr>
<tr>
<td>$c$</td>
<td>Effect of larval competition on survival probability</td>
<td>0.00000866`</td>
</tr>
<tr>
<td>$p_{0}$</td>
<td>Probability of surviving pupation</td>
<td>1.0</td>
</tr>
<tr>
<td>$b$</td>
<td>Proportion of larvae with delayed pupation</td>
<td>0.2</td>
</tr>
<tr>
<td>$b_m$</td>
<td>Proportion of larvae with a fixed bet-hedging strategy</td>
<td>0, 0.2**</td>
</tr>
<tr>
<td>$\delta$</td>
<td>Effect of larval competition on developmental rate</td>
<td>0, 0.3899**</td>
</tr>
<tr>
<td>$a$</td>
<td>Efficiency of adult males to find and mate with females</td>
<td>0.002***</td>
</tr>
<tr>
<td>$t_{m}$</td>
<td>Time per mating</td>
<td>0.333***</td>
</tr>
<tr>
<td>$F_m$</td>
<td>Maximum number of eggs produced per female</td>
<td>28</td>
</tr>
<tr>
<td>$f$</td>
<td>Proportion of females</td>
<td>0.5</td>
</tr>
<tr>
<td>$h$</td>
<td>Harvest rate</td>
<td>0</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>Standard deviation of environmental stochasticity</td>
<td>0.5</td>
</tr>
</tbody>
</table>

- `c` is obtained from Eq. (22) to ensure that larval mortality will keep population at equilibrium; units are larvae$^{-1}$.
- A fixed (unconditional) strategy corresponds to $b_m=0.2$ and $\delta=0$, while a flexible (conditional) strategy corresponds to $b_m=0$ and $\delta=0.3899$. $\delta$ is obtained from Eq (23) to ensure that the proportion of larvae with delayed development is $b$ when the population is at equilibrium.

**Units are area/time. Time unit is the duration of one mating season, i.e. $T=1$.**

$h_m^*$ is 0 as only adult males of the genus Photinus are collected. If harvest rate is sustainable, the number of males at equilibrium will be $A_m^* = (1-f)K(1-h_m^*)$, while the equilibrium number of females will be $A_f^* = fK$. Thus, at a sustainable level of harvest the number of adults will be $A^* = [1-h_m^*(1-f)]K$, which shows that $A^* < K$ when harvest takes place. Consequently, the mean fecundity of females ($F$) will decline with increasing harvest rate of males according to Eq. (8)

$$F = F_m\left(1 - \exp\left(-\frac{a(1-f)KT(1-h_m^*)}{1+at_mK}\right)\right)$$

Therefore, if the harvest rate goes up, the decline in mean fecundity of the females may no longer be sufficient to produce enough males in the next generation for complete female mating, which would further exaggerate the effect of harvest. Consequently, harvest may impose an Allee effect (Allee et al., 1949) on firefly dynamics, which makes the species vulnerable to extinction when harvest rate exceeds a certain threshold. Because harvest reduces the density of mature males, the likelihood that a female will become mated can decrease (Robinet et al., 2007), unless the remaining males can compensate (at least partly) by increasing their mating success. As the parameter $a$ expresses the efficiency of males to mate with females, we analyzed the extinction threshold for three different values of $a$ ($a=0.002, 0.01, and 0.1$).

To investigate how stochasticity affects population persistence of fireflies, we used the stochastic version of the model for two levels of environmental stochasticity ($\sigma = 0.5$ and 1.0) and four harvest rates ($h_m=0, 0.2, 0.4$, and 0.6). We used this wide range of harvest rates because the typical harvest rate of firefly populations is unknown. Rates of 40% and 60% might seem high, but these rates are plausible because fireflies are conspicuous, slow-flying insects that form dense mating aggregations. Default values of the remaining parameters are given in Table 1. All simulations were initiated with a population size close to equilibrium. This was achieved by assuming that all larvae in year 0 were newly hatched; that is, the number of larvae from the previous year was set to 0. With the default parameter values this means that the number of newly hatched larvae must be 66,980 in order to produce 6000 adult fireflies in the following year, while 1500 larvae will stay in the soil for an extra year. The population was then projected for the next 50 years. Each combination of parameter values was replicated 100 times.

2.6. Allowable harvest rate based on survey data

Since detailed life-history data are generally unavailable for fireflies, it might be useful to generate a simple harvest model for a population exposed to environmental stochasticity. We modeled environmental conditions for fireflies in a given year as either good or bad, with reference to the number of adults produced. The probability of a bad year is denoted $\beta$ ($0 \leq \beta < 1$). In a good year, the finite per capita growth rate is $\lambda = (\lambda - 1)$ and in a bad year it is $B = \lambda$, where $B$ defines the effect of a bad year on $\lambda$, i.e. $0 < B < 1$.

We further assumed that $\lambda$ is reduced due to harvest by a factor $1-h_m^*$ where $h_m^* (0 \leq h_m^* \leq 1)$ expresses the effective harvest rate of males. The expected net growth rate over a longer period of time is therefore

$$E[\lambda] = (1-\beta)\lambda(1-h_m^*) + \beta\lambda B(1-h_m^*)$$

As firefly population dynamics are strongly affected by weather conditions (e.g., Yuma, 2007) we set $B=0.3$, which represents the qualitatively estimated decrease in population size associated with a bad year (Faust, unpubl. data). The probability of a bad year ($\beta$) was estimated as 21% using qualitative population data gathered over 19 years from a single population of P. carolinus, a synchronously flashing firefly, in Elkmont, Tennessee, USA (35°39′13″N, 83°34′50″W) (Supplementary Materials). Long-term persistence in a stable environment requires that $E[\lambda] \geq 1$, which implies that the maximum sustainable harvest can be obtained when $h_m^*$ is

$$h_{m,\text{max}} = 1 - \frac{1}{\lambda(1-\beta(1-B))}$$

Using this equation, we estimated the maximum sustainable harvest rate for a range of $\lambda > 1$, and for different combinations of $B$ and $\beta$.

2.7. Sensitivity analysis

Because vital rates and other parameter values used in our model were estimated from a small number of sources, the real-world application of our model conclusions are uncertain. Therefore, we performed a sensitivity analysis to determine which model parameters have the greatest impact on population persistence and therefore have the highest priorities for further research for more accurate assessments. We explored the sensitivity of nine difference parameters by varying them each, one at a time, 10%
above and below their standard value (see Table 2 for parameter values) and examined their effects on the number of males at equilibrium ($A^*$).

3. Results

3.1. Maximum sustainable harvest

Using the deterministic model with male-only harvest before mating ($r = 0$), we found that the sustained yield increased with harvest rate up until a threshold, at which point the population crashed (Fig. 1). Whereas the maximum sustainable harvest is relatively independent of mating efficiency ($a$) at lower harvest rates ($h < 0.2$), the extinction threshold decreases the lower the mating efficiency. Thus, when mating efficiency is high (i.e., $a = 0.1$) the harvest peaks when about 60% of the males are harvested (Fig. 1a), while a harvest rate of about 75% will drive the population to extinction (Fig. 1b). If mating efficiency is ten times lower (i.e., $a = 0.01$), the maximum sustainable yield is only slightly reduced but the population will go extinct if harvest rate exceeds 65%. At the lowest modeled mating efficiency ($a = 0.002$), the maximum sustainable harvest rate is $h = 0.35$, but the population goes extinct when $h = 0.46$. If $a = 0.002$, males in an unexploited population at equilibrium adult population size will, on average, mate twice, which is in agreement with empirical data (Cratsley et al., 2003).

3.2. Demographic and environmental stochasticity

We found that the average population size of adult fireflies and time to extinction decreased with increasing harvest rate and with increasing environmental stochasticity (Fig. 2a–h). Because the simulations were started with the equilibrium number of young larvae ($L^*_0$), the number of larvae increases with a decrease in $\lambda$. Low values of $\lambda$ also increased the time it took to reach a stable number of adults ($A^*$), although a stable level is attained only for the lowest value of $\lambda$ (1.2) when no harvest takes place and environmental stochasticity is low ($\sigma = 0.5$). With no harvest and low environmental stochasticity, average population size tended to reach carrying capacity (Fig. 2a). At the lowest growth rate ($\lambda = 1.2$), population size decreased to zero in every scenario with harvest. Conversely, at the highest growth rate ($\lambda = 2.8$), average population size never declined to zero under any scenario, but it showed more variability when environmental stochasticity ($\sigma = 1.0$) and harvest rate ($h = 0.6$) were high (Fig. 2h). At high harvest rates, only populations with higher growth rates persisted, even with low environmental stochasticity (Fig. 2e and g). Increasing environmental stochasticity in the presence of harvest had the same qualitative effect as when there was no harvest. That is, average population sizes were much lower, and decreased more rapidly over time, with the greatest decreases at the highest harvest rates (Fig. 2d, f and h). The population trajectories in Fig. 2, however, tell only part of the story. For all trajectories except those that attained equilibrium, uncertainty increased over time. This is because the average values depicted include populations that have gone extinct, as well as those that remained near equilibrium. With larger environmental stochasticity and harvest rates, there is increasing extinction risk over time, although higher growth rates increased the probability of population persistence (Fig. 3a–b).

3.3. Effect of larval developmental strategy

We compared developmental strategies when a population is exposed to moderate harvest ($h_m = 0.4$) in a stochastically variable environment ($\sigma = 1.0$) (Fig. 4). When larval development cannot be prolonged (when $b = 0$), 92% of the simulated populations persisted after 50 years. This percentage tends to increase with $b$ for the flexible conditional (density-dependent) strategy but decreases sharply for the fixed (unconditional) strategy. This clearly indicates that the flexible developmental strategy is much more robust against extinction than is the fixed strategy (Fig. 4). The difference between the two strategies is exaggerated in the more unpredictable environment.

3.4. Allowable harvest rate based on survey data

For estimating allowable harvest rate when all one has is survey data, we needed the probability of bad years and the effect of a bad year on population size (Eq. (27)). Using the data available to us, the maximum sustainable harvest rates for a range of $\lambda s > 1$ and a range of environmental variances ($\sigma \geq 0$), are shown in Fig. 5. Maximum harvest rates based on survey data for P. carolinus suggest that effective harvest rates >10% are sustainable only if $\lambda > 1.4$, and that higher environmental variance decreases the average maximum sustainable harvest rate (Fig. 5).

3.5. Sensitivity analysis

The parameters that caused the greatest changes in equilibrium population size were larval survival probability ($p_m$), maximum number of eggs per female ($F_m$), and egg hatching probability ($p_e$) (Table 3). There were also strong asymmetric effects of pupation survival probability ($p_p$) and larval competition’s effect on survival probability ($c$); decreases in the former had a strong effect in decreasing equilibrium population size, while increases in the latter caused a strong increase. When changed by 10%, all parameters with the exception of the effect of larval competition on survival probability ($c$), had a greater effect on decreasing the population than on increasing the population.

4. Discussion

Habitat loss and degradation have contributed to declining firefly populations in some regions (Khooh et al., 2009; Wong and Yeap, 2012). In Japan, the well-documented decline of Luciola cruciata

Fig. 1. (a) The predicted harvest and (b) number of adults ($A^*$) in the population when exposed to harvest rate ($h$) for different values of mating efficiency ($a$). $A^*$ is equal to the carrying capacity ($K$) when no harvest takes place. This is under the assumption that males are harvested before they have the chance to mate.
has been attributed to habitat destruction, light pollution, commercial harvest, and water pollution (Katoh et al., 2009; Ohba, 2004; Yajima, 2007; Yuma, 2007). In some parts of the world fireflies are harvested, and regardless of a species’ life history, a sufficient harvest rate can cause population declines. The big question is what harvest rate causes declines for a particular species? Results from our stochastic simulation model suggest that Photinus firefly populations can sustain only moderate levels of male harvest. Specifically, in our models, high environmental stochasticity coupled with high harvest rates invariably led to rapidly declining populations no matter what growth rate was assumed. A population could tolerate higher harvest rates under lower environmental stochasticity, but only the highest growth rates enabled the modeled population to persist for 50 years. Because of the widespread availability of recombinant luciferase, it is no longer necessary to harvest fireflies to obtain luciferase. Although our model was able to predict sustainable levels of harvest for Photinus populations, its validity depends on the accuracy of our estimates of Photinus vital rates. Because not even qualitative data are available on firefly harvest and growth potential, the applicability
of our results cannot be validated at this time. As population persistence was highly influenced by growth rate estimates, this is one of the most important areas for future firefly research. Better estimates of population sizes, and how they change across years, are also necessary for accurately determining persistence likelihood and sustainable harvest rates of fireflies.

To determine biologically sustainable commercial harvest rates for any firefly species, we recommend that statistically valid survey plots be established to document the relationship between harvest rate and firefly population sizes across a range of ecological conditions, and better and more accurate vital rates need to be determined for effective harvest. Lessons might be extrapolated from successful harvest programs for other taxa (e.g., Breitburg et al., 2000; Emanuel et al., 2005; Punt and Smith, 2000). In addition, based on our sensitivity analyses, we encourage researchers to gather more demographic data in the field. Specifically, it would be particularly important to determine values for probabilities of larval survival ($p_m$), pupation survival ($p_p$), and egg hatching probability ($p_e$), as well as maximum eggs produced per female ($F_m$). We realize that this will be challenging and possibly expensive, and that the methods might not yet exist to determine values for some species. For example, virtually nothing is known about the fraction of larvae spending more than one year in the soil under natural conditions; similar cryptic life stages are present in other species of firefly as well (e.g., Luciola cruciata, Takeda et al., 2006).

![Fig. 3](image1.png)  
**Fig. 3.** Effect of different annual harvest rates ($h$) on the probability of modeled adult firefly populations persisting over the course of 50 years with an environmental stochasticity $(\sigma)$ of 0.5 (a) or 1.0 (b). Each line represents a different value of $\lambda$ (from 1.2 to 2.8). Each case was replicated 100 times; means are plotted without error bars for clarity.

![Fig. 4](image2.png)  
**Fig. 4.** Population persistence as a function of percent of larvae postponing pupation. The fixed strategy assumes that the percent of larvae with prolonged development is independent of larval density (i.e., $\delta = 0$) while the flexible strategy assumes that it is density-dependent (i.e., $\delta > 0$). Environmental stochasticity $(\sigma)$ is set to 1.0 and the effective harvest rate of males ($h_{fa}$) is set to 0.4. See Table 1 for the remaining parameters.

![Fig. 5](image3.png)  
**Fig. 5.** Estimated average allowable harvest rate using only data on growth rate $\lambda$ (Eq. [28]), probability of a bad year ($\delta = 0.21$), and effect of a bad year on growth rate ($B = 0.30$). Environmental stochasticity $(\sigma)$ at 0 (bold line), 0.5 (dashed line), and 1.0 (dotted line) are presented for a range of $\lambda_s > 1$. 

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### Table 3

Relative rank of each variable's effect on decreasing and increasing the number of males at equilibrium ($A^*$), $A^* = 4118$ under standard conditions.

<table>
<thead>
<tr>
<th>Variable</th>
<th>$A^*$</th>
<th>% change</th>
</tr>
</thead>
<tbody>
<tr>
<td>$p_m$</td>
<td>2907</td>
<td>29.4</td>
</tr>
<tr>
<td>$p_p$</td>
<td>2969</td>
<td>27.9</td>
</tr>
<tr>
<td>$r_m$</td>
<td>3499</td>
<td>15.0</td>
</tr>
<tr>
<td>$p_e$</td>
<td>3499</td>
<td>15.0</td>
</tr>
<tr>
<td>$c$</td>
<td>3674</td>
<td>10.8</td>
</tr>
<tr>
<td>$b$</td>
<td>3914</td>
<td>5.0</td>
</tr>
<tr>
<td>$l/t_m$</td>
<td>3997</td>
<td>2.9</td>
</tr>
<tr>
<td>$h$</td>
<td>4094</td>
<td>0.6</td>
</tr>
<tr>
<td>$r$</td>
<td>4114</td>
<td>0.1</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Variable</th>
<th>$A^*$</th>
<th>% change</th>
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<tr>
<td>$p_m$</td>
<td>4974</td>
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<td>$c$</td>
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<tr>
<td>$r_m$</td>
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<td>$b$</td>
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<tr>
<td>$l/t_m$</td>
<td>4207</td>
<td>2.2</td>
</tr>
<tr>
<td>$h$</td>
<td>4147</td>
<td>0.7</td>
</tr>
<tr>
<td>$r$</td>
<td>4123</td>
<td>0.1</td>
</tr>
</tbody>
</table>
Determining some of these values even in captivity might be challenging.

One interesting result from our model is the importance of the larval emergence strategy. Because adults only live for a single season, a population without a risk-spreading strategy ($b = 0$) faces extinction if bad weather in one year prevents females from reproducing. When we allowed larvae to postpone pupation, we found that a fixed (unconditional) strategy performed worse than did a strict one-year lifecycle. Spending an extra year in the soil, a flexible, density-dependent strategy, was superior with respect to buffering environmental uncertainty, despite increased mortality due to intraspecific competition and cannibalism (Fig. 4). The proximate cause of this increased persistence is that between-year variation in number of adults is stabilized, because in a year with many larvae, a relatively large fraction postpones pupation to the following year, while the opposite will be the case in a year with few larvae. Such a mechanism reduces the risk that the number of adults in a given year will reach a critical threshold below which the population is likely to go extinct (see below). This relationship could be mediated by body size, as increased density results in increased food competition, and many insect species delay pupation until they reach a certain body size (Beaudoin et al., 1992; Matsuoka, 2006; Teng and Apperson, 2000).

Although our model shows that the fixed developmental strategy seems to be unable to buffer environmental stochasticity, this does not imply that a bet-hedging (fixed development) strategy cannot occur in this species. If prolonged development is balanced by some advantages, it could be maintained. Thus, in our simulations we assumed that larvae staying two years in the soil suffered higher larval mortality than did those staying only a single year. This may not be the case if prolonged larval development is caused by diapause (e.g. Danks, 1992; Menu et al., 2000), as diapausing larvae do not compete for resources and therefore are not at risk from food shortages. At the same time, diapausing larvae would not exert a negative influence on the non-diapausing larvae. There is evidence from laboratory studies that firefly larvae can enter diapause during periods of low food availability (McLean et al., 1972). This difference between active and inactive larvae could be modeled via the competition coefficients $c_p$ in Eq (5). Another possibility is that larvae with postponed development continue to grow, which may explain why both small and large larvae can be found at the same time (Buschman, 1984; McLean et al., 1972). If adults that hatch from larger larvae have higher reproductive success than do the small larvae, it could offset a higher mortality encountered during prolonged larval development. In contrast, a phenotypically plastic larval development response could increase population persistence if it buffered environmental stochasticity (Grimm et al., 2005).

Another aspect of firefly life history that needs further empirical investigation is the relationship between the number of adult males and the chance that females become mated. Mating probability likely decreases with population size, in particular with the number of adult males. Low mating success can exert an Allee effect (Gascoigne et al., 2009; Yamakawa and Liebhold, 2009), thus making small populations more vulnerable to extinction. Fig. 1 indicates that the separation between maximum sustainable harvest and extinction caused by harvest is rather narrow, especially if $A$ is small. Consequently, stochastic events may push a population that is harvested at close to the maximum sustainable rate, into the unstable region and eventual extinction.

Of the field data needed for firefly population viability and harvest rate assessment, standardized monitoring (Kirton et al., 2012; Takeda et al., 2006) would be the most readily achievable. From these time-series data one could calculate annual variation in population size and growth rates ($\lambda$), which could provide estimates of the amount of environmental stochasticity these animals are facing. Monitoring and management programs have been established in the Great Smoky Mountains National Park (Faust, 2010; Faust and Weston, 2009) Allegheny National Forest, PA (Faust et al., 2012) and Congaree National Forest, SC (Faust, pers. comm). Because of their popularity with the public, fireflies might also benefit from data gathered by a citizen science program. As an example, “Firefly Watch” is a citizen science initiative sponsored by the Boston Museum of Science (https://www.mos.org/fireflywatch/, accessed 21.06.2010) that provides one approach to collecting and managing such data. This program encourages citizens across North America to monitor the number of fireflies appearing in their backyards during the spring and summer months. This approach might not be as statistically rigorous as other survey designs, but in their absence it would provide useful data on firefly abundance and distribution.

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**Appendix A. Supplementary data**

Supplementary data associated with this article can be found, in the online version, at http://dx.doi.org/10.1016/j.ecolmodel.2013.02.018.

**References**


PA. In cooperation with the U.S. Forest Service, Department of Agriculture, American Naturalist 155, 724–734.